As a student do I need to know or remember my European Student Identifier

No need for that. The ESI is a technical identifier and is generated electronically and maintained by your own university.